

# Energy Scale References

## D0 Escale references:

- NIM article (hep-ex/9805009)
- Other D0 talks/notes: [www-d0.fnal.gov/daniel/jesgroup/jesgroup.html](http://www-d0.fnal.gov/daniel/jesgroup/jesgroup.html)

## Other sources of interest:

- CDF Z->B-BBAR (Jets + tracks)
  - <http://home.fnal.gov/~dorigo/thesis.ps>
  - [http://home.fnal.gov/~dorigo/jet\\_corr.ps](http://home.fnal.gov/~dorigo/jet_corr.ps)
- ALEPH Energy Flow NIM A 360 (1995) 481

Q1: What's a Jet?

all jet analyses must begin with this question

After defining the jets (choosing algorithm) the scale may be chosen

Energy Scale

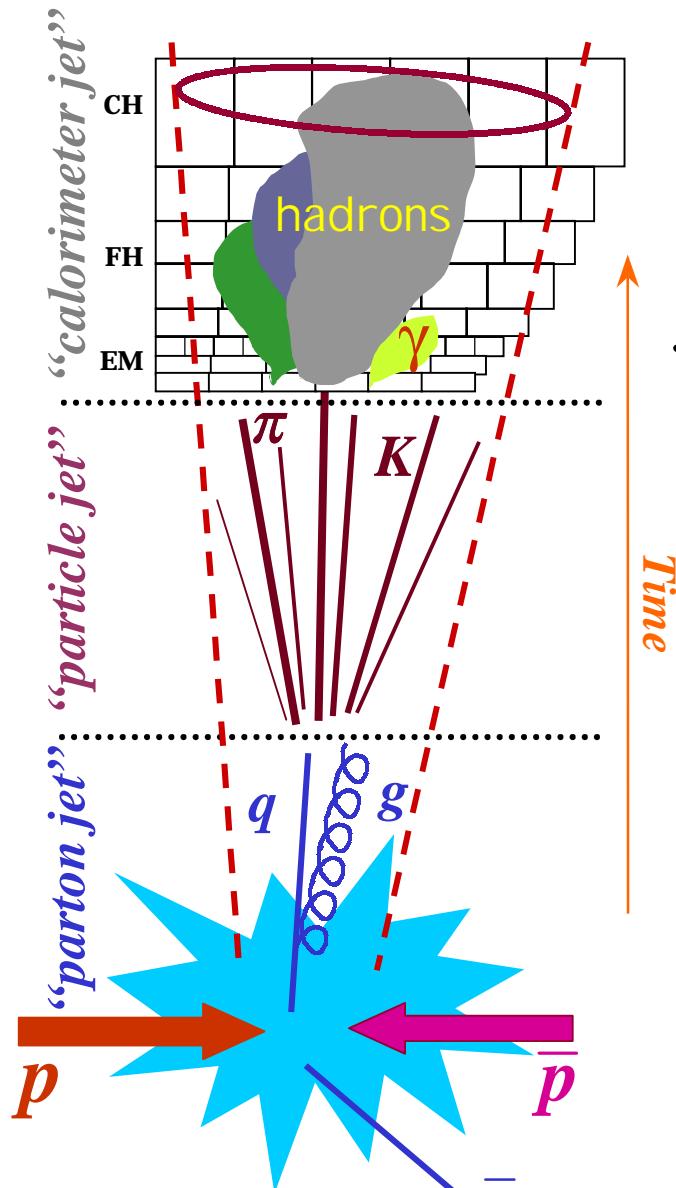
A: Equivalence of particle Energy to Detector Energy

Momentum Scale

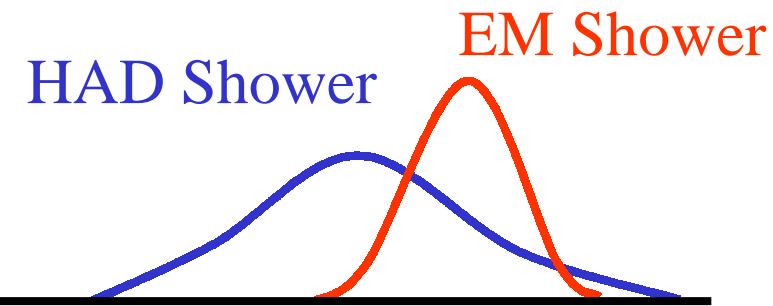
B: Equivalence of particle Momentum to Detector Momentum

# Single Particle Response

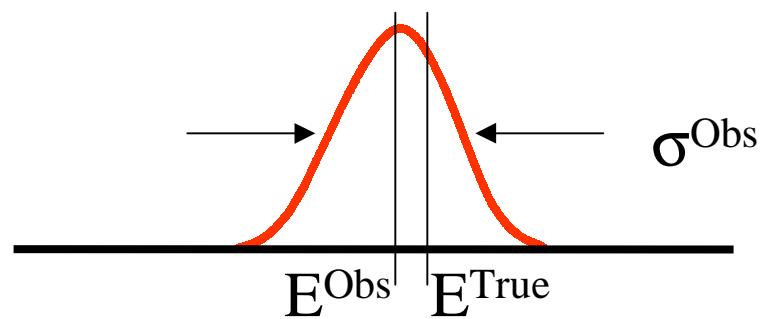
Leakage?



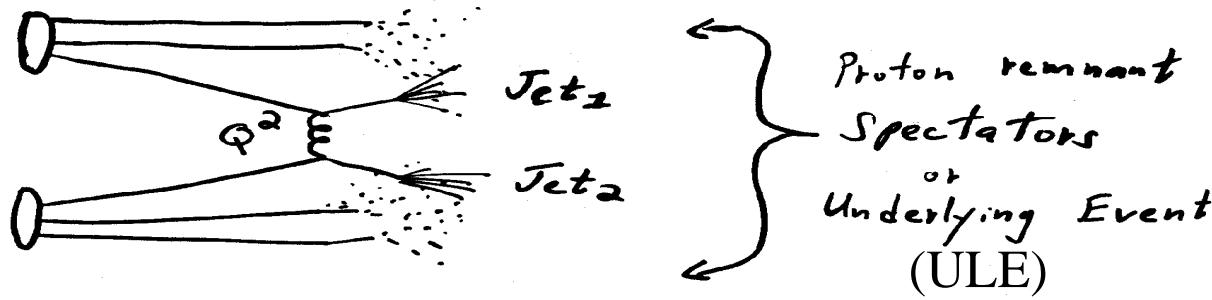
Jets are  $\sim \langle 1/3 \rangle$  EM-like, increasing with  $\ln(E)$



Jet response in hermetic detector  
CLT at work...

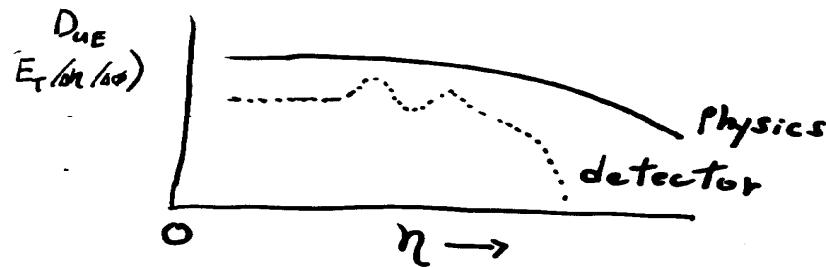


Jet scale moves  $\langle E^{\text{obs}} \rangle$  to  $\langle E^{\text{obs}} \rangle$   
And ideally reduces overall  $\sigma$



## Back to Q1: What's (in) a Jet?

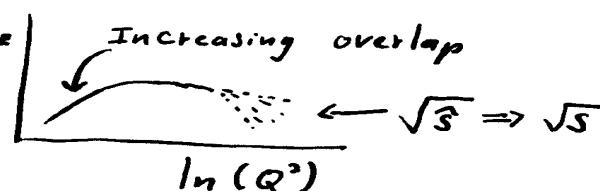
Run I choice (ULE) is not part of jet,  
subtract on average based on jet algorithm +  $\eta$ .



Density of ULE  
(Min Bias Model)  
 $\langle E_T \rangle / \text{on}/\text{off}$

Alternate choices:

- Include ULE in jet energy
- Define ULE ( $Q^2$ ) Due



For some recent studies of ULE in various MC and data samples see:  
Fermilab-Pub-00/297 contrib. of Field&Stuart

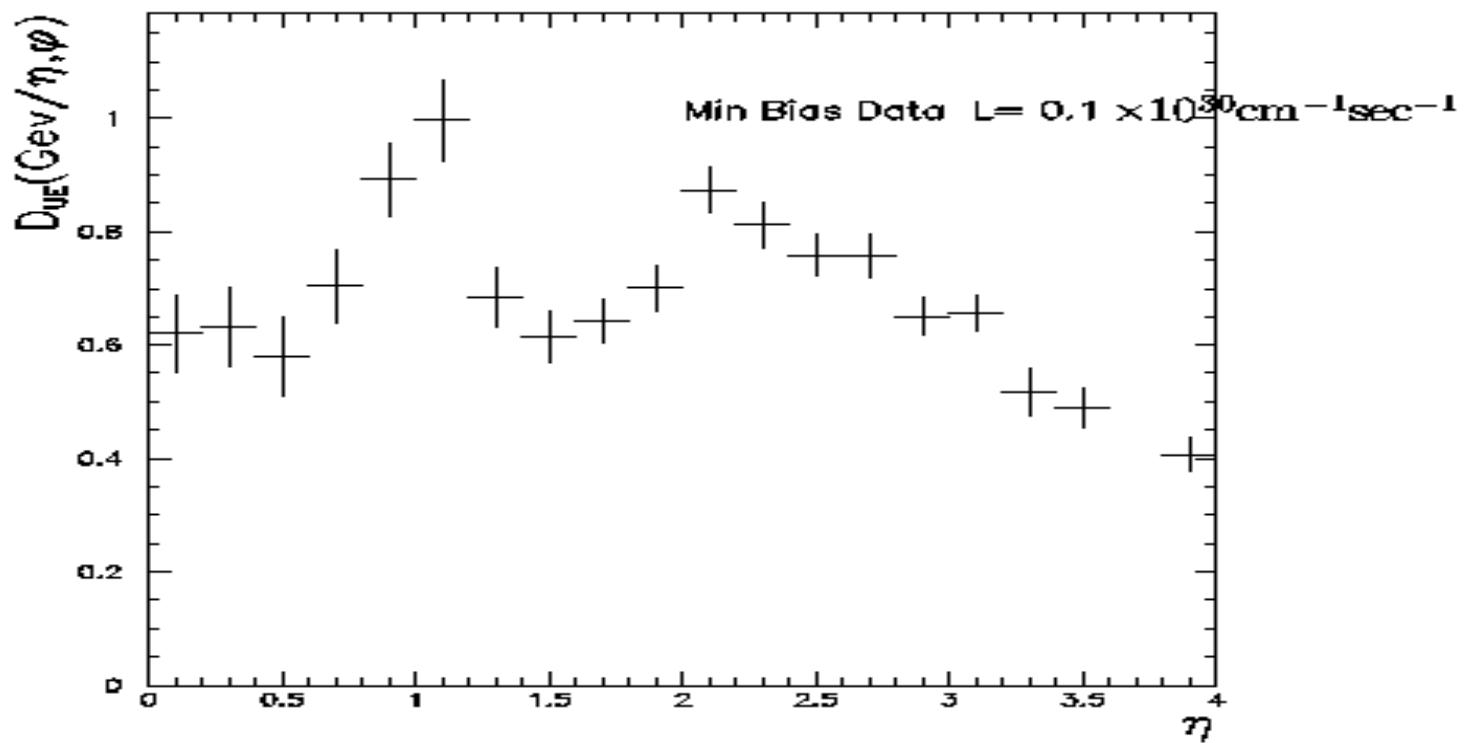
## Offset Correction

$$E_T^O = E_T^{ue} + E_T^\Theta$$

$$E_T^O = E_T^{ue} + \langle N_{extra} \rangle E_T^{ue} + E_T^{noise} + E_T^{pile}$$

$E_T^{ue}$  underlying event from spectator interactions associated with the hard collision that caused the trigger

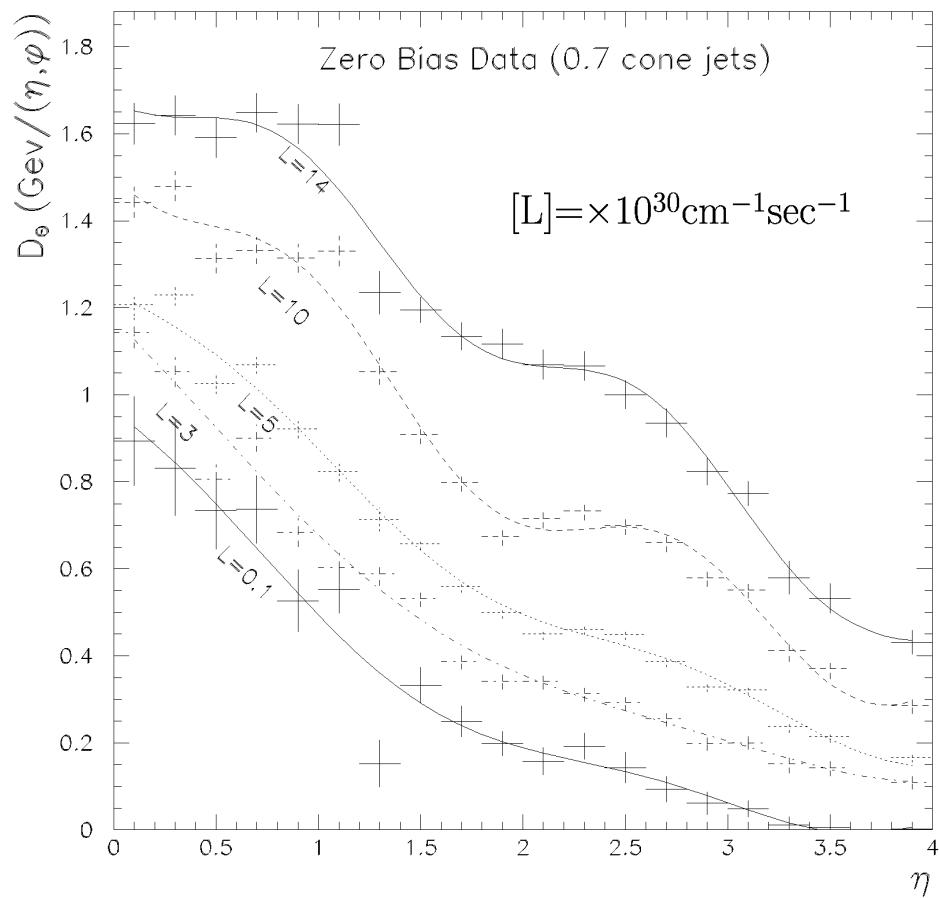
$E_T^\Theta$  Ur noise, pile-up and extra  $p\bar{p}$  interactions



Use low luminosity MIN BIAS and ZB (no Hard Collision) data:  $D_{ue}(\eta) = D_{MB}(\eta) - D_{ZB}^{no HC}(\eta)$

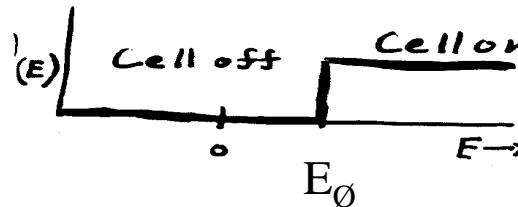
Noise, pile-up and extra  $p\bar{p}$  contributions  
from ZB data in different luminosity bins:

$$D_\Theta(L, \eta) = D_{ZB}(L, \eta)$$



# Subtraction of ULE (+noise & pileup)

Complicated by zero suppression effects



Cell readout is  
Zero suppressed

$$\sum_{\text{Cells}} E_{\text{jet}} \Theta(E_{\text{jet}}, E_\theta) + E_{\text{noise}} \Theta(E_{\text{noise}}, E_\theta) + E_{\text{ULE}} \Theta(E_{\text{ULE}}, E_\theta)$$

$$\neq \sum_{\text{Cells}} E_{\text{Total}} \Theta(E_{\text{Total}}, E_\theta)$$

$E_{\text{jet}}$  is not a simple subtraction

$$E_{\text{jet}} = E_{\text{Total}} - \langle E^{\text{ULE}} \rangle - \langle E^{\text{noise}} \rangle - \underline{O_c(E, \eta, L)}$$

The offset correction depends on occupancy.

Run I (cone): develop empirical occupancy correct from data to get back  $E_{\text{jet}}$

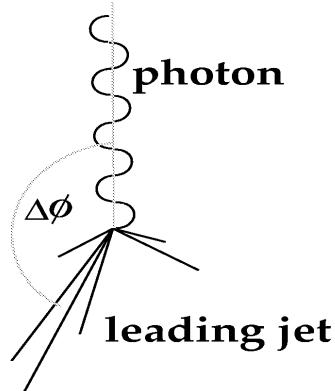
Run I ( $k_T$ ): Overlay noise + ULE + generated jets  
apply ZSP in software + directly measure effect on jets  $\star$

# Response Correction

Jet Response is typically  $< 1$ .

- $h/e \neq 1$
- Uninstrumented regions
- Module to module fluctuations

## Missing $E_T$ Projection Fraction Method



Based on event energy balance  
in the transverse plane

In an ideal calorimeter:

$$\vec{E}_{T\gamma} + \vec{E}_T^{had} = 0$$

In the DØ calorimeter:

$$R_{em}\vec{E}_{T\gamma} + R_{had}\vec{E}_T^{had} = -\vec{p}_T$$

Once photons are calibrated,  $R_{em} = 1$ :  $R_{had} = 1 + \frac{\vec{p}_T \cdot \hat{n}_{T\gamma}}{E_{T\gamma}}$

For a  $\gamma$ -jet two body process:  $R_{jet} = R_{had}$

To avoid resolution bias and effect of a  
steeply falling  $\gamma$  cross section:

$R_{jet}$  versus  $E'$       with       $E' = E_{T\gamma} \cosh(\eta_{jet})$

$E' \rightarrow E_{jet}^{meas}$       and       $R_{jet}$  versus  $E_{jet}^{meas}$

(  $E_{T\gamma}$  and  $\eta_{jet}$  measured with good resolution)

# Cryostat Factor Correction

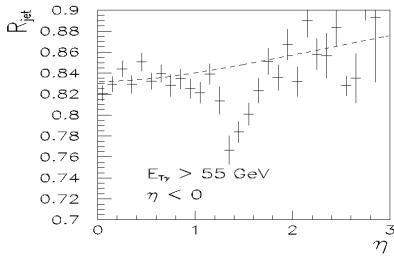
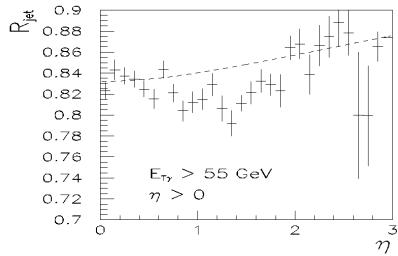
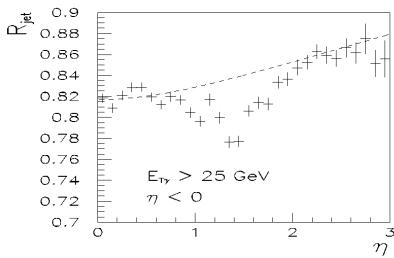
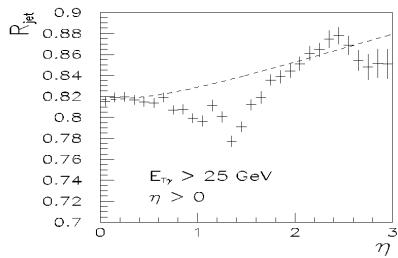
$F_{cry}$ : Ratio of  $R_{jet}^{EC}$  over  $R_{jet}^{CC}$

SAME TECHNOLOGY  $\Rightarrow F_{cry}$  flat as a function of  $E'$

- Calibrate EC with respect to CC
- Use EC points to extend the energy reach of CC measurement

=Detector uniformity corrections

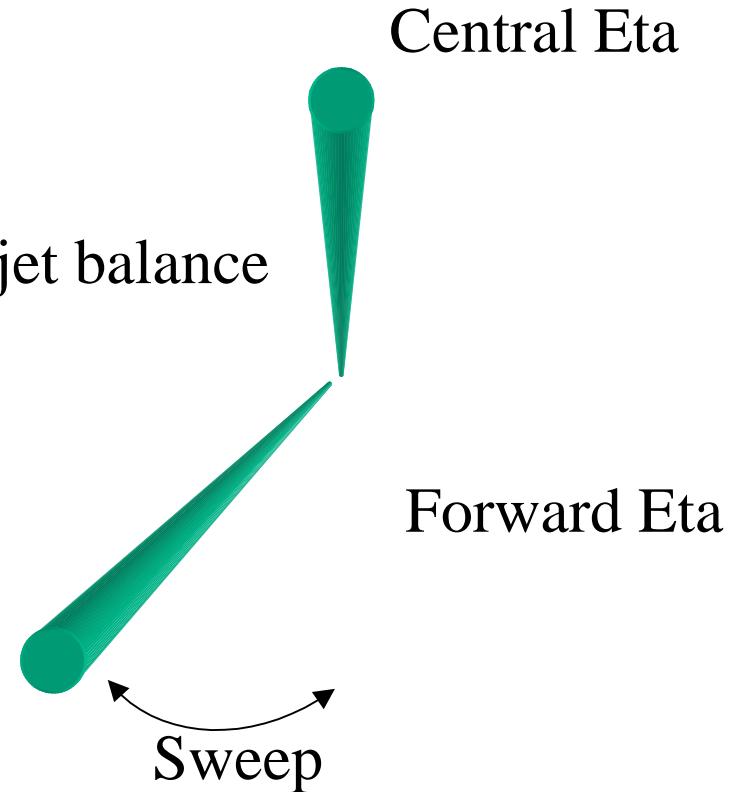
$\eta$  Dependent Correction,  $F_\eta$



$$R_{jet} = \alpha + \beta \cdot \ln(E) \Rightarrow R_{jet} = a + b \cdot \ln[\cosh(\eta)]$$

$F_\eta$  correction defined as the difference between

EXPECTED  $R_{jet}$  and MEASURED  $R_{jet}$  in the IC



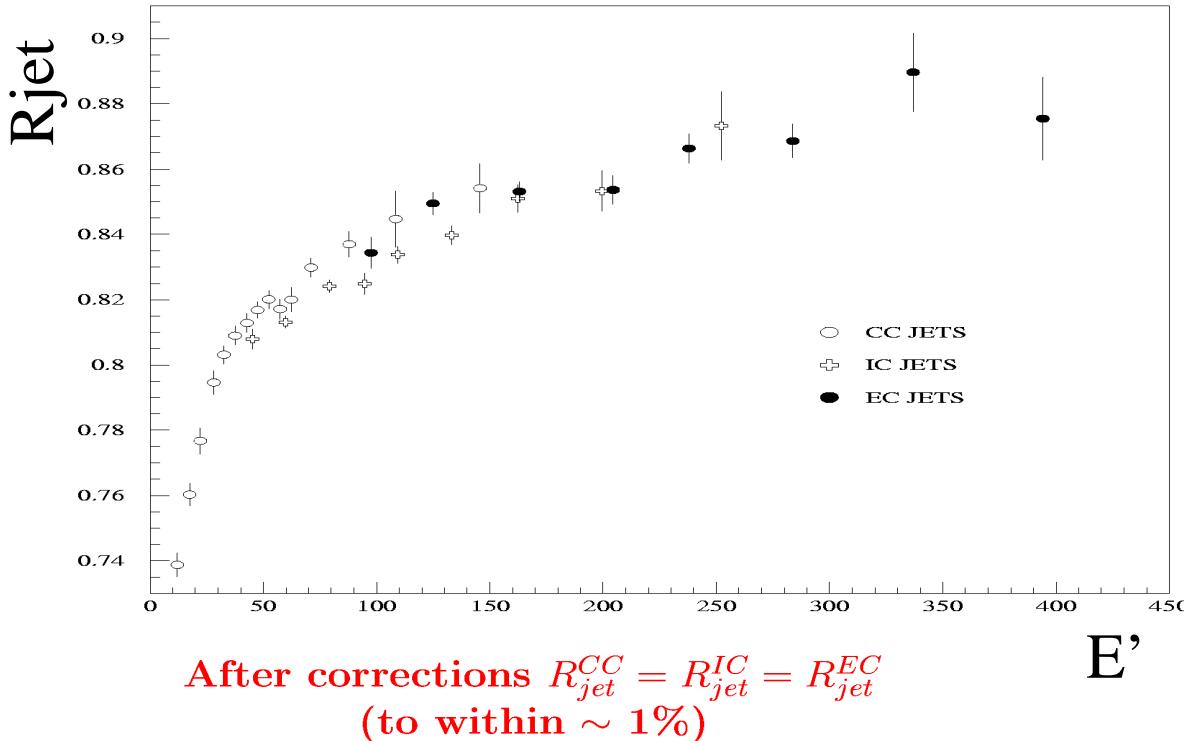
# CC Response Measurement

$F_{cry}$  and  $F_\eta$  make the Calorimeters “UNIFORM”:

- Apply offset correction to  $E_{Tjet}^{meas}$  ( $\vec{H}_T$  STAYS THE SAME)
- Apply  $F_{cry}$  and  $F_\eta$  to  $E_{Tjet}^{meas}$  and  $\vec{H}_T$

$$E_{Tjet}^{corr} = E_{Tjet}^{meas} \times F_{cry} \times F_\eta$$

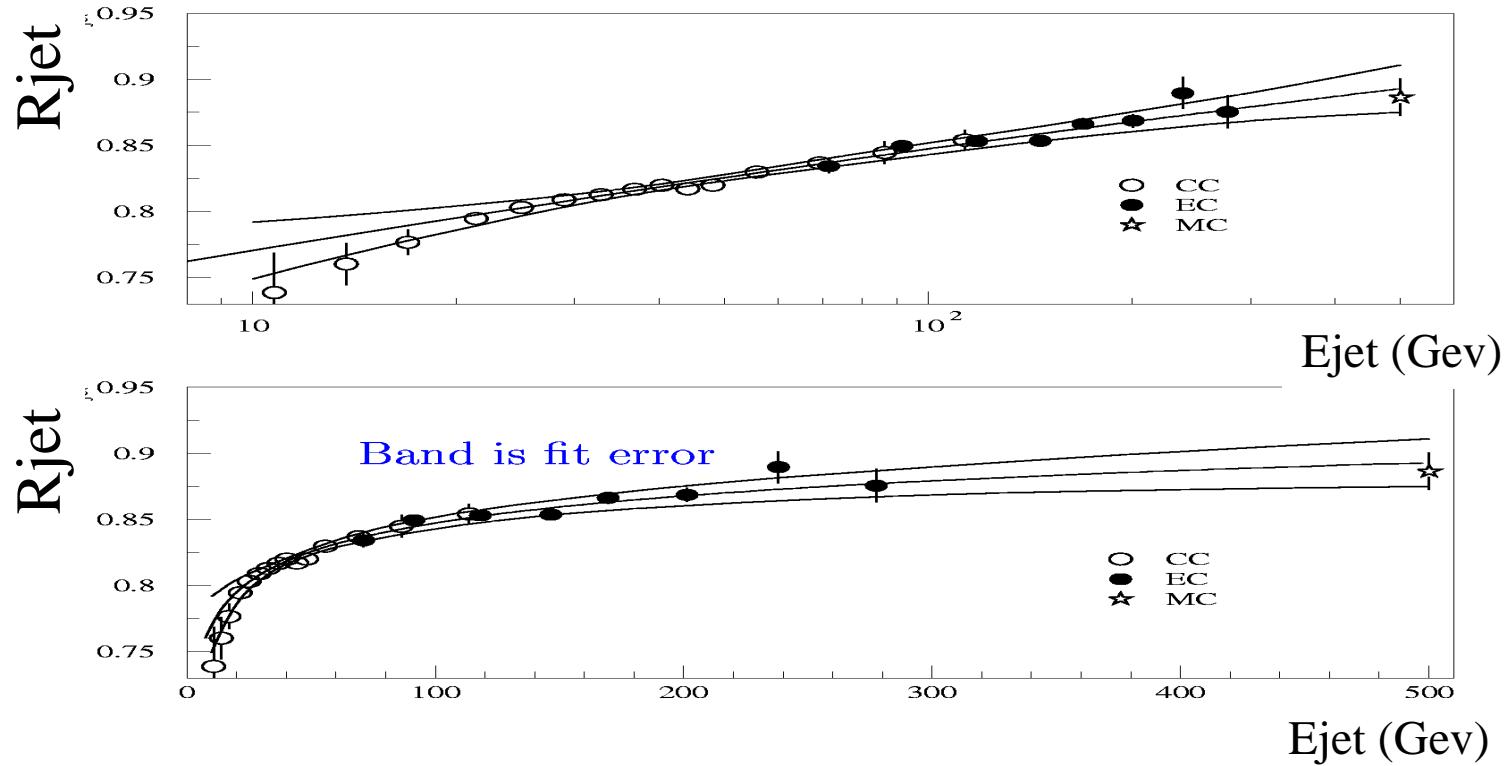
$$\vec{H}_T^{corr} = \vec{H}_T^{meas} + \sum_\gamma \vec{E}_{T\gamma}^{meas} - \sum_\gamma \vec{E}_{T\gamma}^{corr} + \sum_{jet} \vec{E}_{Tjet}^{meas} - \sum_{jet} \vec{E}_{Tjet}^{corr}$$



# $R_{jet}$ versus $E_{jet}$

If  $h/e \neq 1 \Rightarrow \pi/e \sim 0.1 \times \ln(E(GeV))$

$$R_{jet} = A + B \cdot \ln(E_{jet}) + C \cdot [\ln(E_{jet})]^2$$



CC, EC points used below 300 GeV

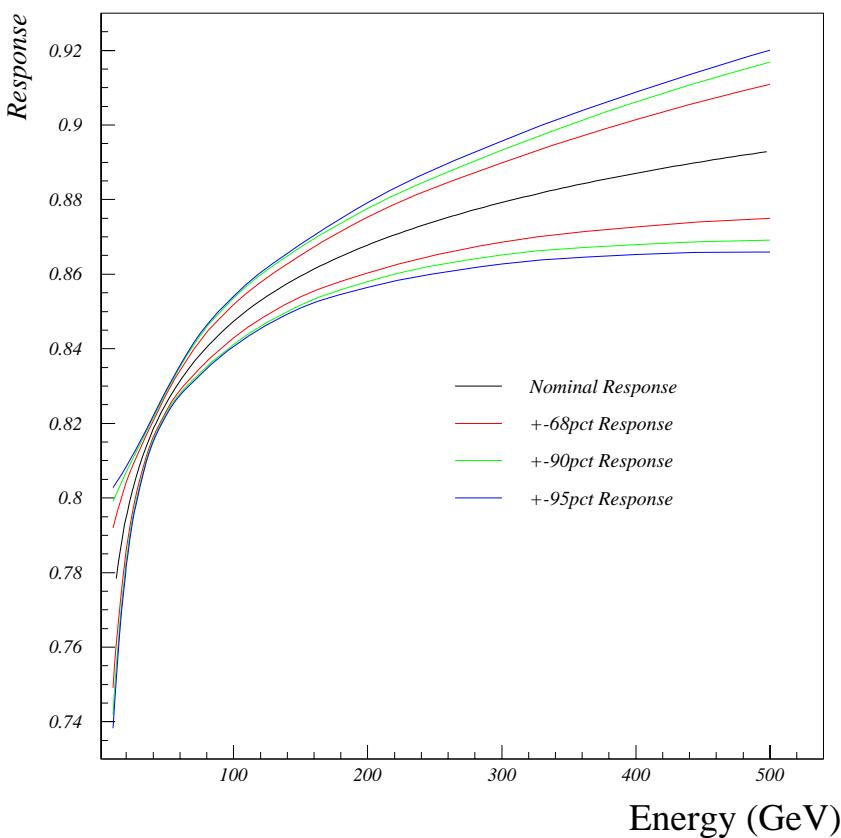
MC point (hybrid data set) from convolution of HERWIG jet events and Test Beam single particle response:

Shape of  $R_{jet}^{data}$  and  $R_{jet}^{hyb}$  agree at high  $E_{jet} \Rightarrow$   
use MC point to constrain the fit

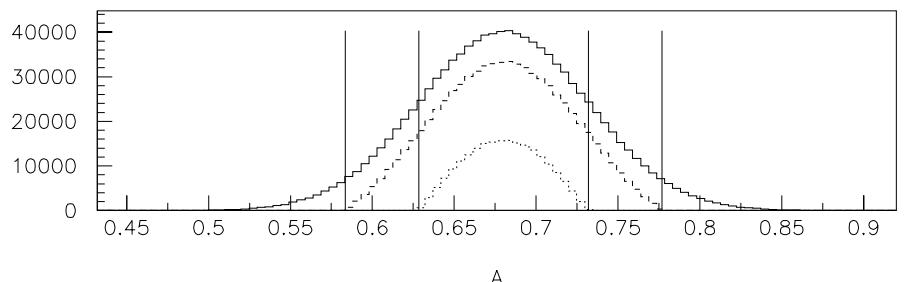
# A more detailed look at Response

Sample probability distribution for fit parameters:

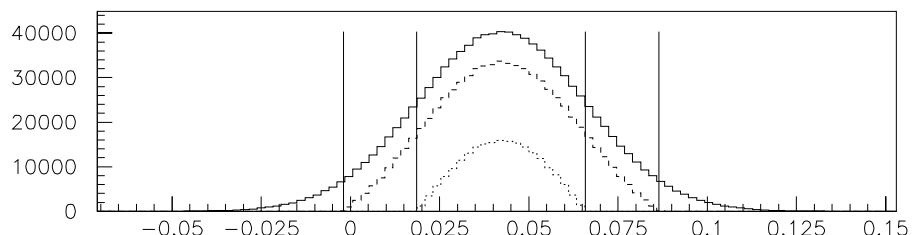
This distribution contains information for allowed response shapes and their relative likelihoods



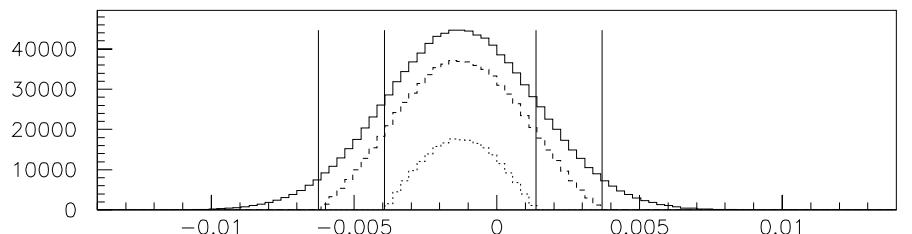
Outer bands - 68% CL, all params. free  
Inner bands - 68% CL, 1 param. free



A

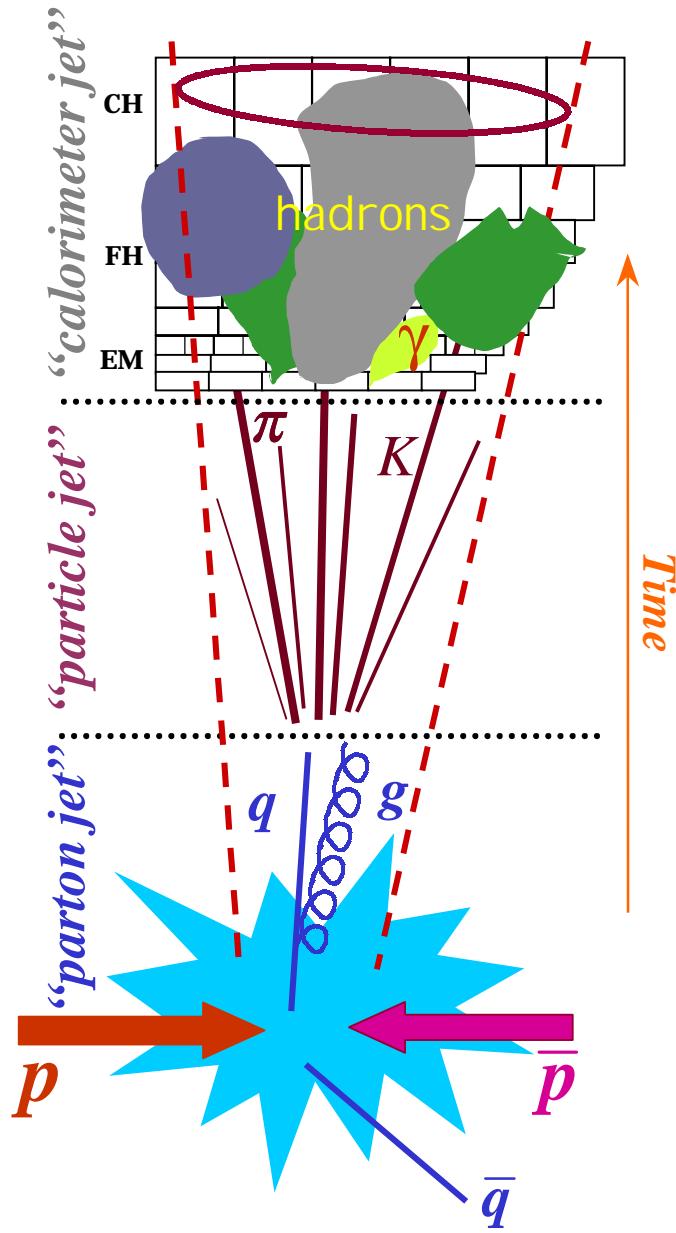


B



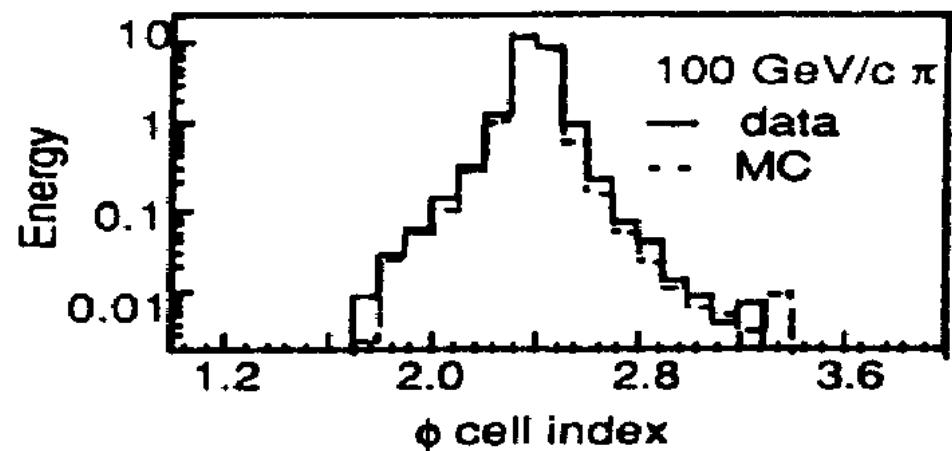
C

# Showering



Particles emitted inside cone, but depositing energy out of cone in detector

Opposite effect can also occur leading to energy showering into cone



Transverse shower shape, 100 GeV pions

# Showering

Method:

- Test your MC against jet and single particle profiles
- (un)Correct particle-level jets for detector response to get the detector energy associated w/the particle jets
- Compare fraction of this detector energy that lies w/in the jet cone (in the detector) to total detector energy

This compensates for energy showered into/out of the cone.

But...

MPF method bias effects can cause double correction

$$R_{had} \equiv 1 + MPF = 1 + \frac{\vec{E}_T \cdot \hat{n}_T^\gamma}{E_T^\gamma}$$

Missing  $E_T$  in direction of photon  
can be biased by widely  
showering jets

Solution involves some ‘tuning’ of limits for following particle showers

# Some words about RunII

New opportunities w/ E/P measurement from tracker may be helpful for lower PT jets – MPF method still superior for high PT

Determine offset corrections from MB data + MC jets

Revisit solutions for MPF bias in showering correction

Separate b-jet scales ( $Z \rightarrow b\bar{b}$ , gamma+bjet)

Work underway on EFLOW type corrections